

How do we use completing the squares to find centers & radii?

Do Now Solve for x by completing the square

$$x^2 - 6x + 5 = 0$$

$$x^2 - 6x + 9 = -5 + 9$$

$\div 2 \swarrow \quad \searrow \uparrow \times 4$
 $-3 \quad -3 \quad 9$

$$(x - 3)^2 = 4$$

$$x - 3 = \pm 2$$

$$x = 3 \pm 2 \begin{cases} \rightarrow 3 + 2 \\ \rightarrow 3 - 2 \end{cases}$$

$$x^2 + 4x + y^2 - 6y = 5$$

$$\underbrace{x^2 + 4x + 4}_{\div 2 \swarrow \quad \searrow \uparrow \times 4} + y^2 - 6y + 9 = 5 + 4 + 9$$

$\div 2 \swarrow \quad \searrow \uparrow \times 4$
 $2 \quad -3 \quad 9$

$$(x + 2)^2 + (y - 3)^2 = 18$$

$$(x - h)^2 + (y - k)^2 = r^2$$

center: $(-2, 3)$

radius: $\sqrt{18} = 3\sqrt{2}$

$$x^2 + 6x - 5 + y^2 - 2y = 3$$

Find center, radius, area, circumference.

$$(x^2 + 6x + 9) + (y^2 - 2y + 1) = 3 + 5 + 9 + 1$$

$$(x+3)^2 + (y-1)^2 = 18$$

$$A = \pi r^2$$

$$= \pi(18) = 18\pi$$

$$(-3, 1)$$

$$r = \sqrt{18} = 3\sqrt{2}$$

$$C = \pi D$$

$$= 6\sqrt{2} \pi$$

$$(x+1)^2 = x^2 + 2x + 1$$

$$(x+2)^2 = x^2 + 4x + 4$$

$$(x+3)^2 = x^2 + 6x + 9$$

$$(x+4)^2 = x^2 + 8x + 16$$

$$(x+5)^2 = x^2 + 10x + 25$$

Find the center & radius of

$$2x^2 + 4x + 2y^2 + 6y = 8$$

$$\frac{x^2 + 2x + 1}{+y^2 + 3y + 2.25} = -4 + 1 + 2.25$$

$$(x+1)^2 + (y+1.5)^2 = 7.25$$

$$C: (-1, -1.5)$$

$$r = \sqrt{7.25}$$